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# **Wave-Domain Adaptive Filtering for Acoustic Human-Machine Interfaces based on Wavefield Analysis and Synthesis**

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**Multimedia Communications and Signal Processing**  
University of Erlangen-Nuremberg

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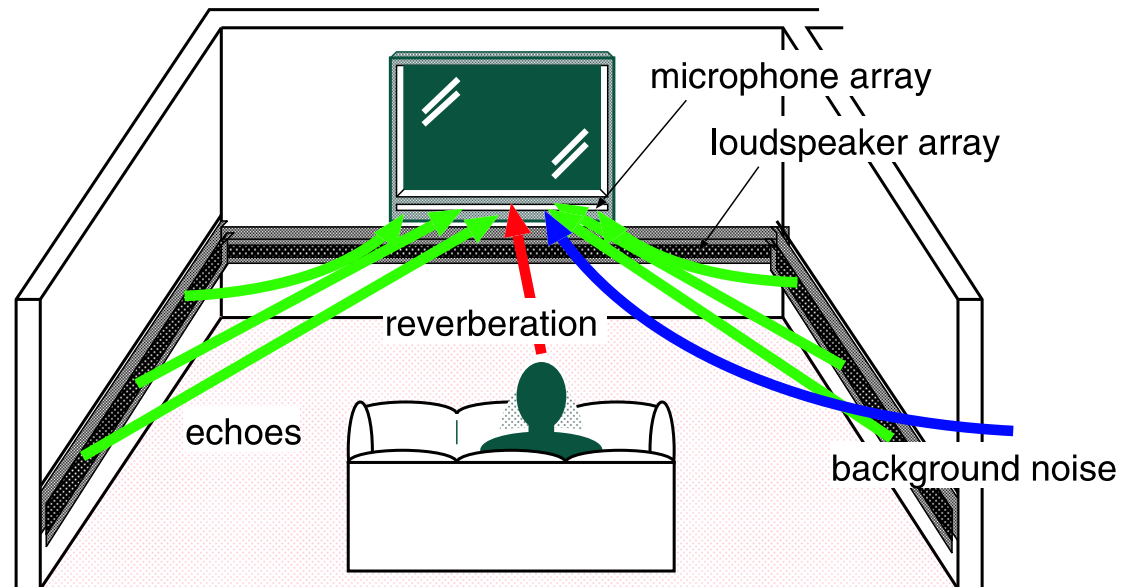
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- Background: Conventional point-to-point adaptive multichannel processing
- Novel approach: Wave-Domain Adaptive Filtering (WDAF)
- Evaluation of WDAF for acoustic echo cancellation
- Summary and outlook

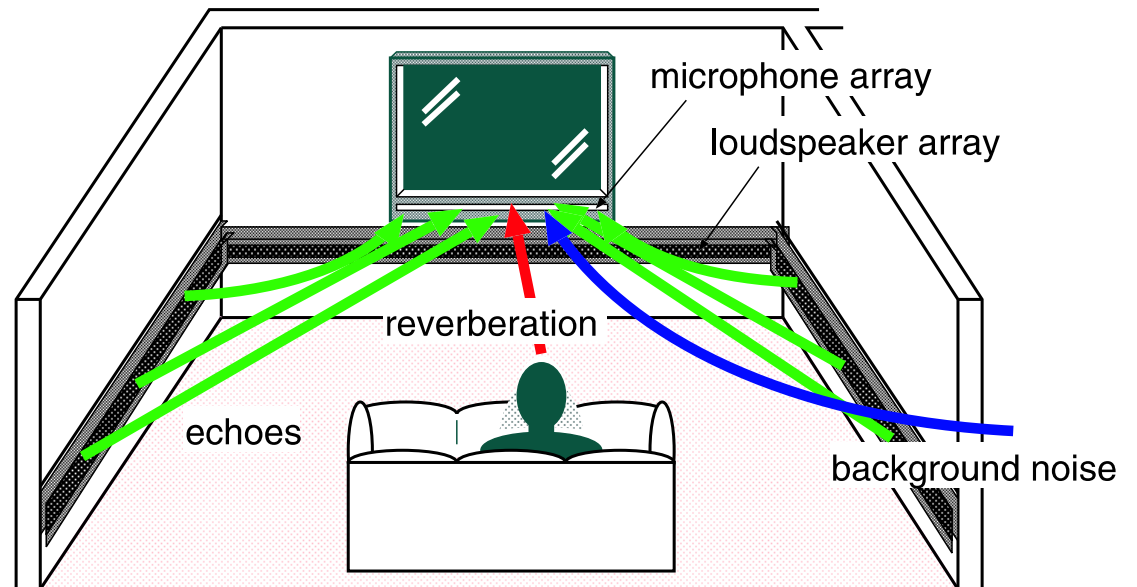
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- **Multichannel reproduction:**  
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- **Multichannel recording:**  
⇒ microphone array processing



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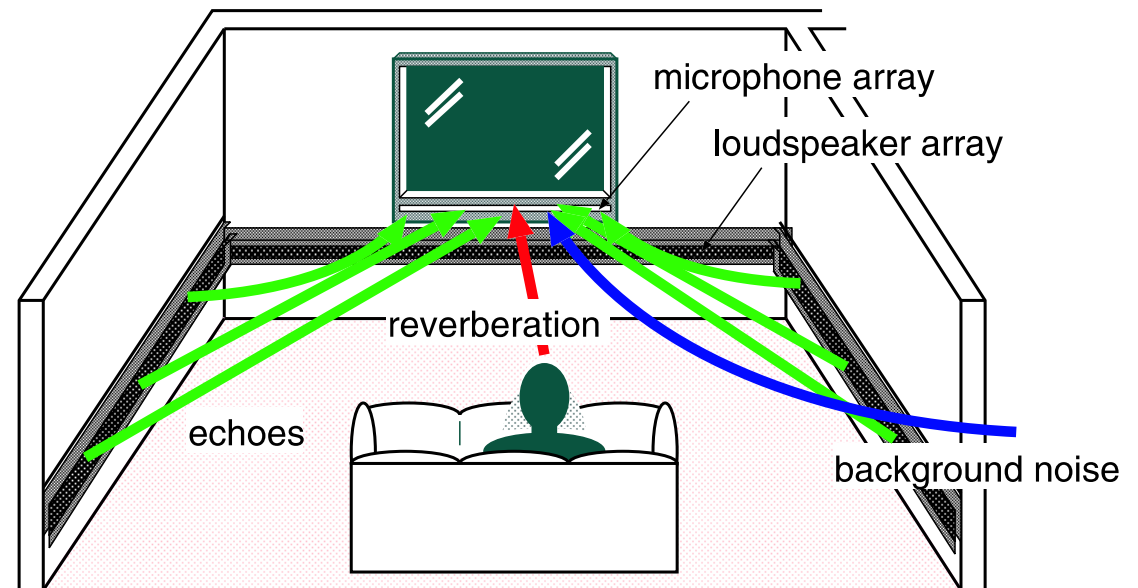
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**Major challenge:** adaptive signal processing for massive multichannel systems

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**Major challenge:** adaptive signal processing for massive multichannel systems

**We propose:**

framework for efficient spatio-temporal transform-domain adaptive filtering exploiting foundations of wave physics:

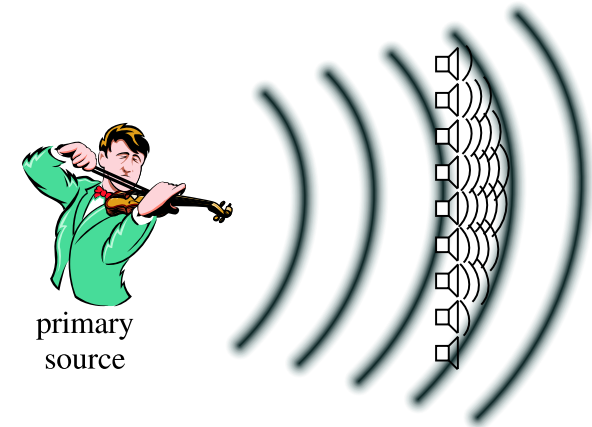
**Wave-Domain Adaptive Filtering**

# Motivation (2): Wave-Field Synthesis and Wave-Field Analysis

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## Huygens (1690):

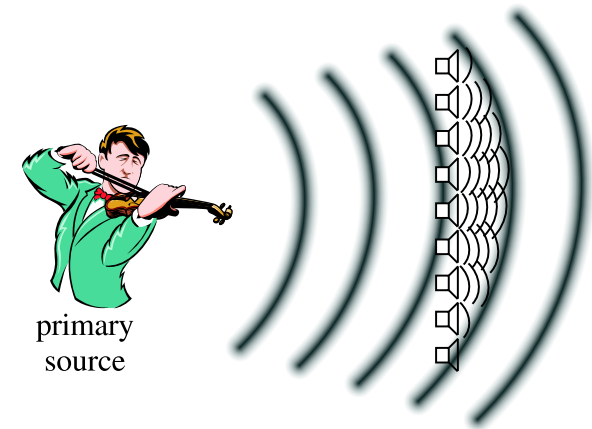
Any point on a propagating wavefront can be taken as a point source for the production of spherical secondary waves.



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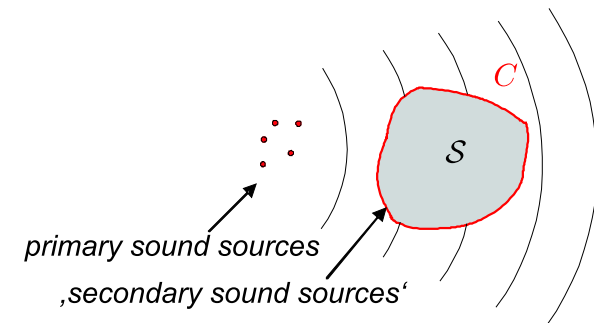
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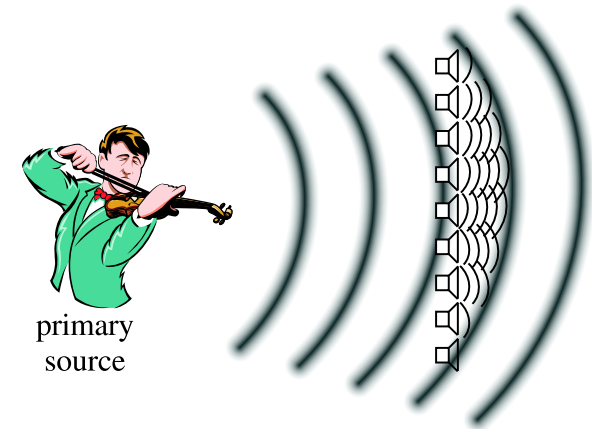
At any listening point within the source-free listening area  $S$ , the sound pressure field  $p(\mathbf{r}, t)$  can be calculated if both, the *sound pressure and its gradient are known on the contour  $C$*  enclosing this area.



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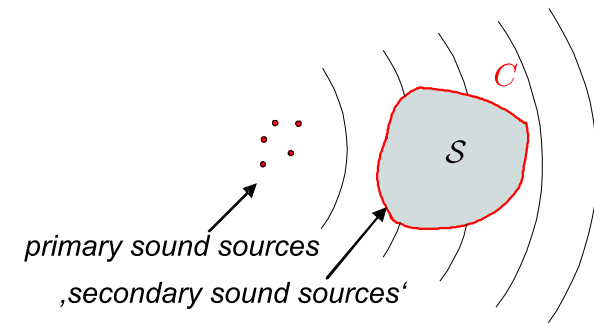
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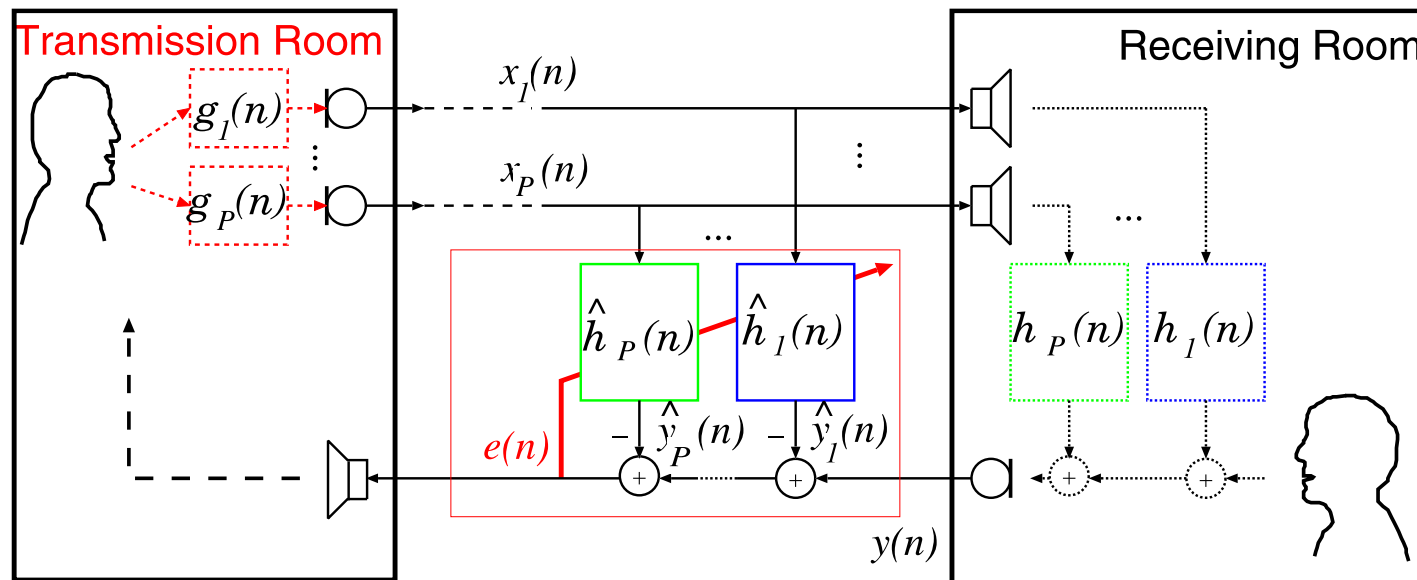
## Practical realization:

WFS and WFA by spatial sampling using loudspeaker arrays and microphone arrays, resp.  $\Rightarrow$  **large number of loudspeaker and microphone channels**



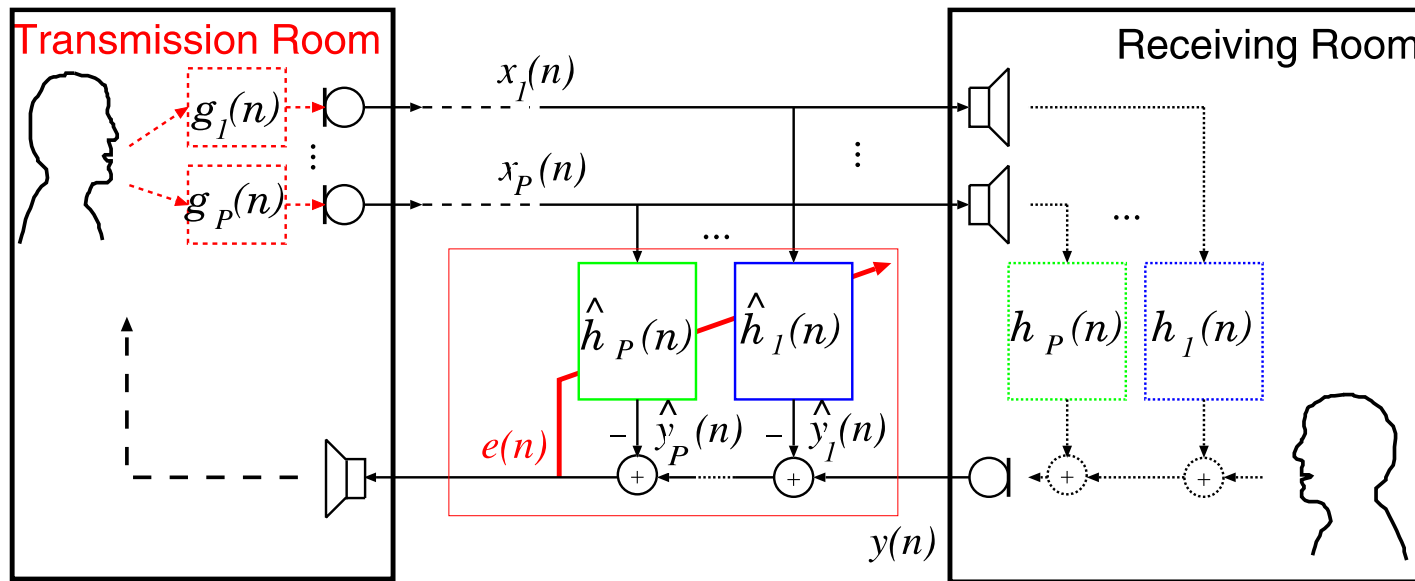
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## Prominent example: multichannel acoustic echo cancellation (AEC)



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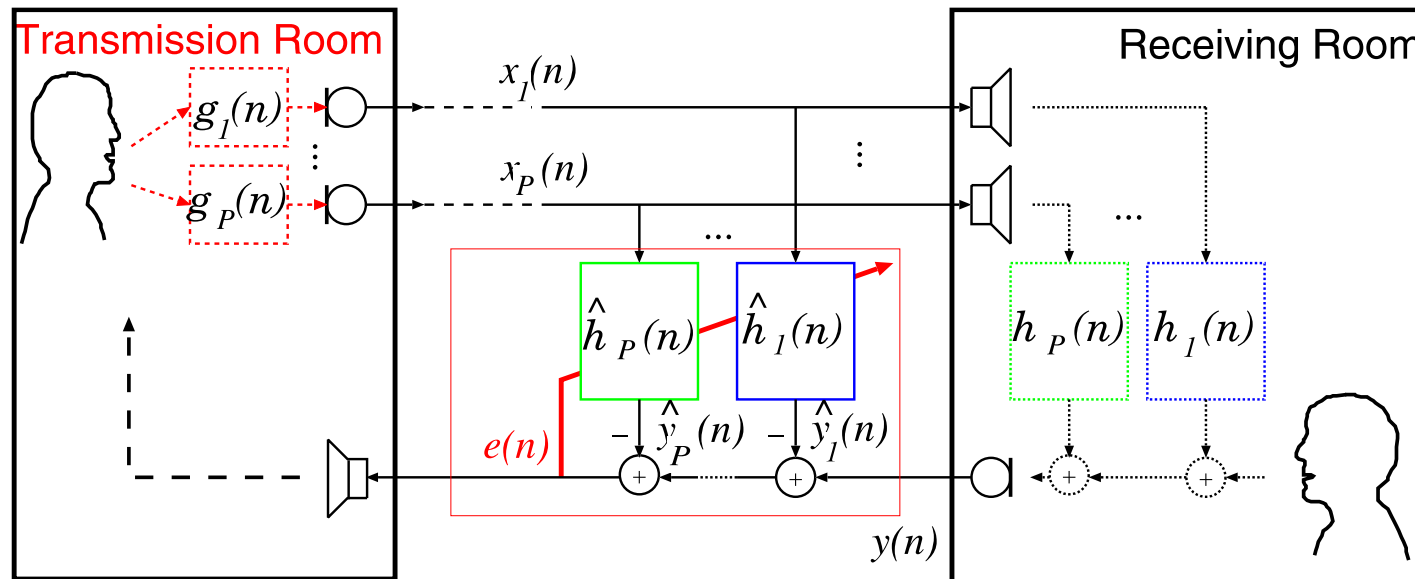
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⇒ adaptive system identification

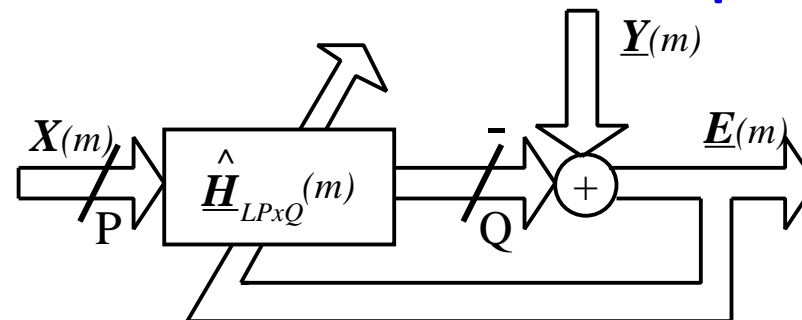
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## Generalization: adaptive FIR MIMO filter with $P$ inputs and $Q$ outputs



# Background: Point-to-Point Adaptive Multichannel Processing (2)

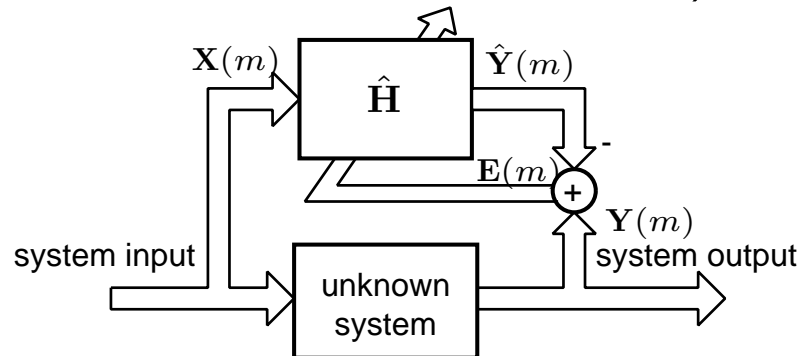
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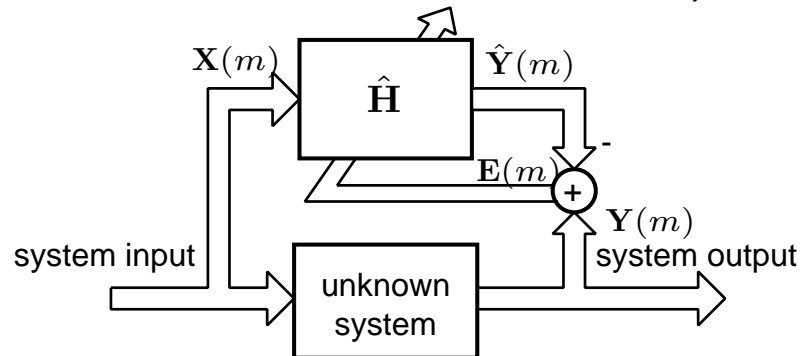
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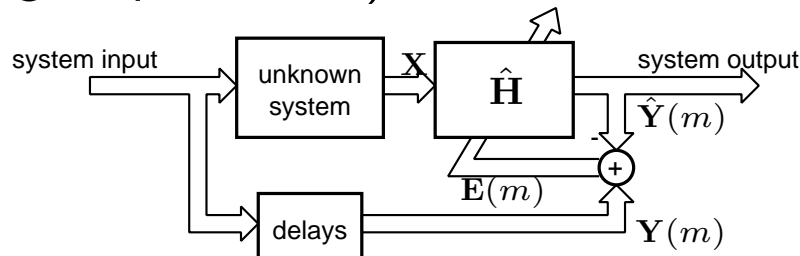
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## Adaptive Filtering Constellations (multichannel version of [Haykin]):

- **System identification**  
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- **Inverse modeling**  
(e.g., equalization)

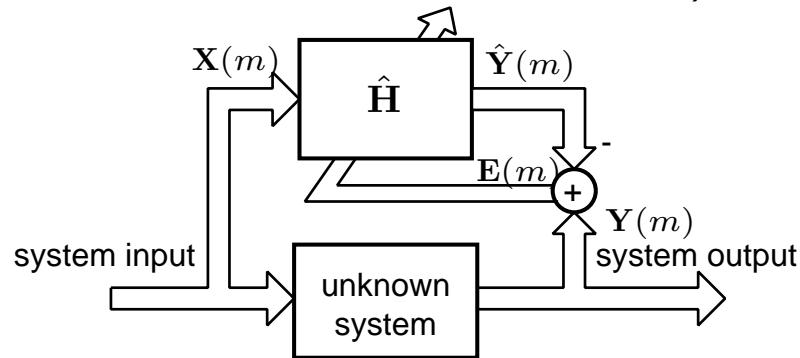


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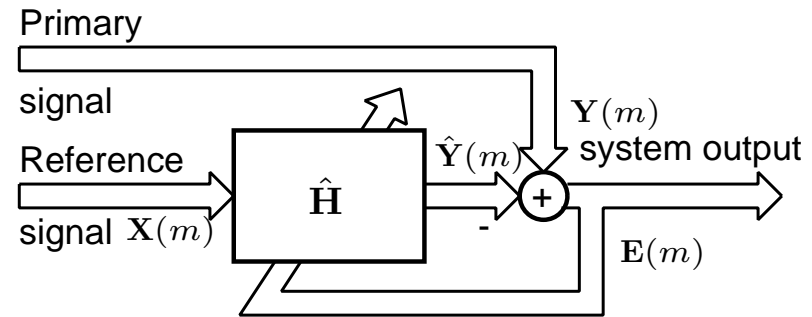
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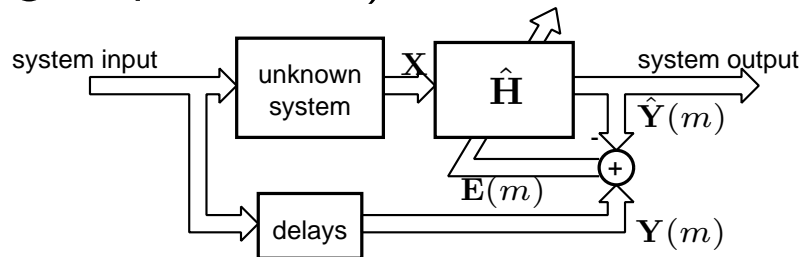
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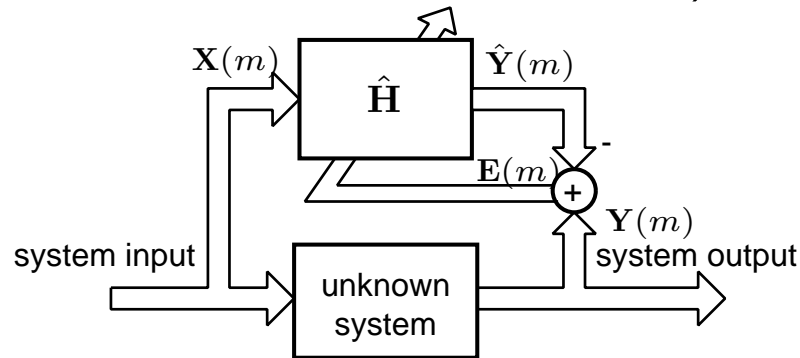


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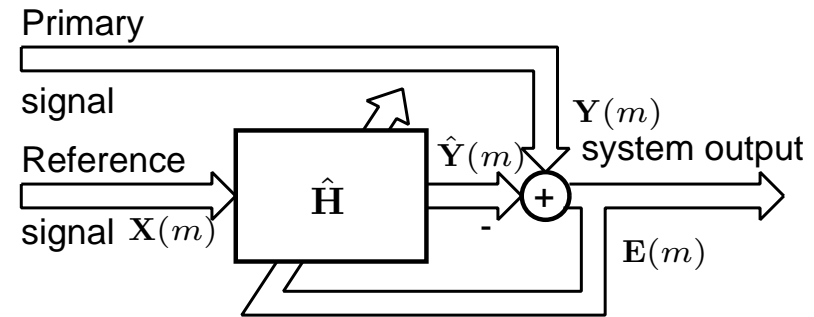
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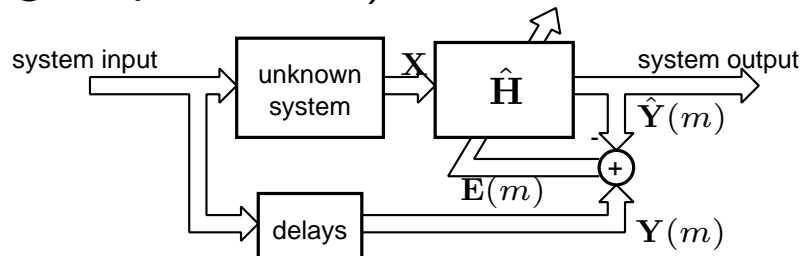
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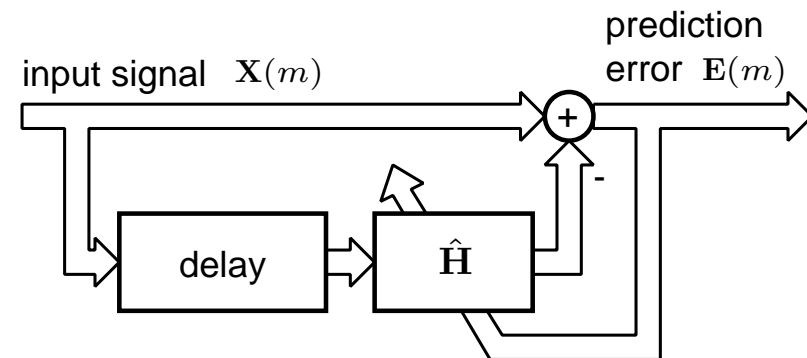


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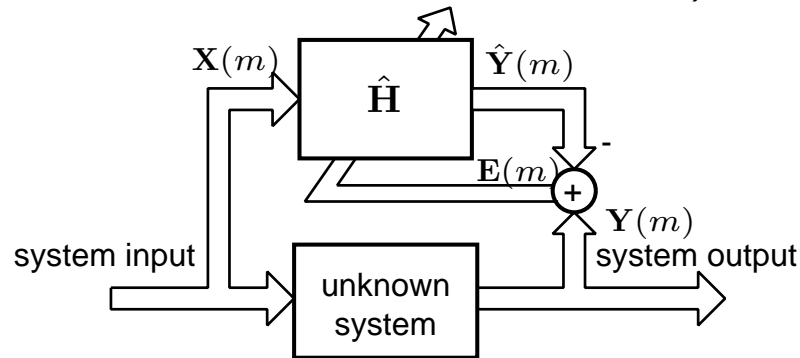


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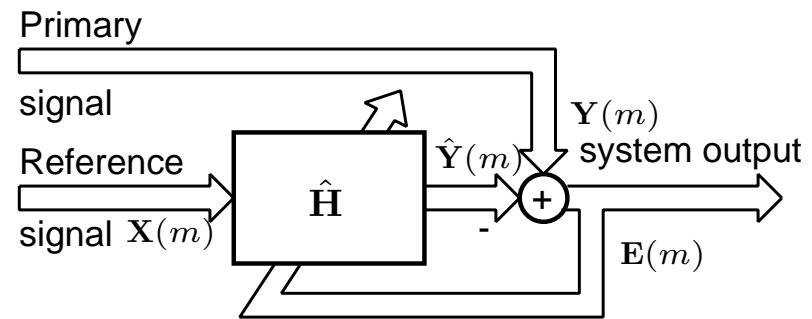
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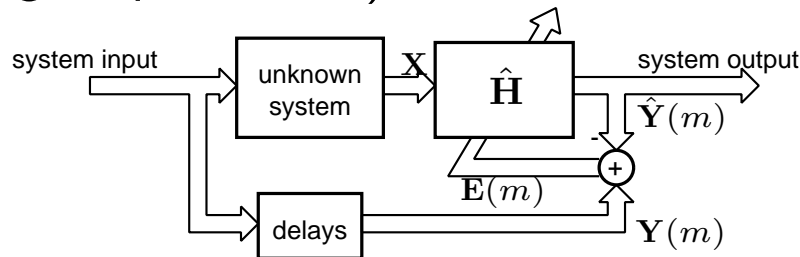
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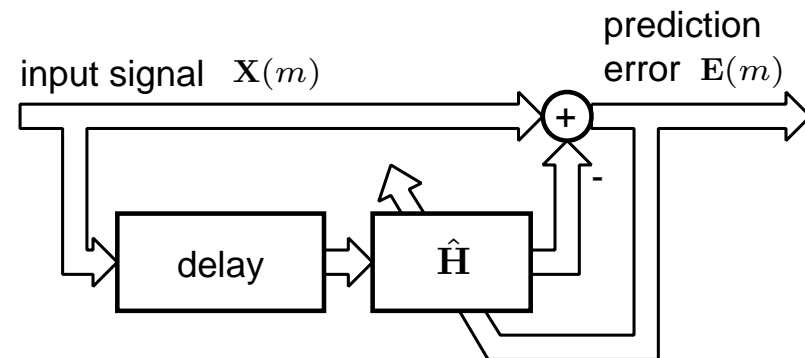


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⇒ **Least-Squares problems**, adaptive solutions with continuous updates for tracking

# Multichannel Adaptive Filtering for Solving the LS Problem

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Most known adaptation algorithms (e.g., LMS/NLMS) exhibit slow convergence for highly correlated input signals.

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Theoretically Optimum Solution: **Multichannel Recursive Least-Squares (MC RLS)**

$$\begin{aligned} \mathbf{e}(n) &= \mathbf{y}(n) - \hat{\mathbf{H}}^T(n-1)\mathbf{x}(n) \\ \hat{\mathbf{H}}(n) &= \hat{\mathbf{H}}(n-1) + \mathbf{R}_{\mathbf{xx}}^{-1}(n)\mathbf{x}(n)\mathbf{e}^T(n) \end{aligned} \quad \begin{array}{l} \text{with input correlation matrix} \\ \mathbf{R}_{\mathbf{xx}}(n) = \begin{bmatrix} \mathbf{R}_{\mathbf{x}_1\mathbf{x}_1}(n) & \cdots & \mathbf{R}_{\mathbf{x}_1\mathbf{x}_P}(n) \\ \vdots & \ddots & \vdots \\ \mathbf{R}_{\mathbf{x}_P\mathbf{x}_1}(n) & \cdots & \mathbf{R}_{\mathbf{x}_P\mathbf{x}_P}(n) \end{bmatrix} \end{array}$$

- all correlations taken into account by (large) matrix  $\mathbf{R}_{\mathbf{xx}}^{-1}(n) \Rightarrow$  rapid convergence
- computationally very expensive
- in practice often numerical problems

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**Multichannel Frequency-Domain Adaptive Filtering (MC FDAF)**

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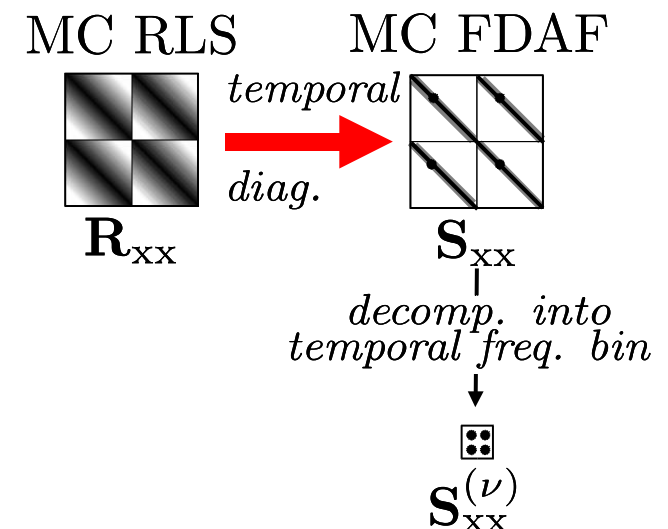
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**Multichannel Frequency-Domain Adaptive Filtering (MC FDAF)**

- **approximate diagonalization** of the correlation matrices  $\mathbf{R}_{\mathbf{xx}}$  by DFT
- very efficient use of the FFT  
 $\Rightarrow$  gains for both, adaptation and filtering
- there are algorithms fully taking into account all cross-correlations using  $\mathbf{S}_{\mathbf{xx}}^{(\nu)}$



# Massive Multichannel Systems

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For massive WFS-based multichannel applications:

- High complexity

Example (Echo cancellation for typical 48-channel WFS-based system):

$$P \cdot Q \cdot L = 48 \cdot 48 \cdot 1024 = 2304 \cdot 1024 = 2359296 \text{ filter taps to optimize}$$

- Even bin-wise matrices  $\mathbf{S}_{xx}^{(\nu)}$  become large and ill-conditioned

⇒ Current algorithms cannot be used

⇒ Is there a more "global" point of view?

# Novel Approach: Wave-Domain Adaptive Filtering (WDAF)

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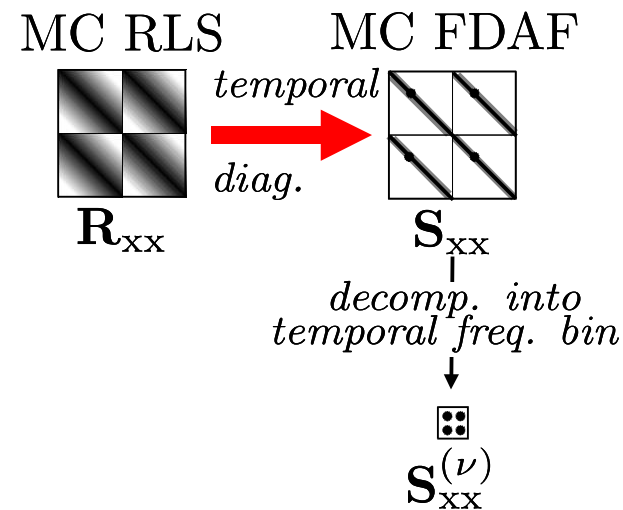
## Basic concept:

- give up point-to-point model  
(→ ordinary difference equation) in  
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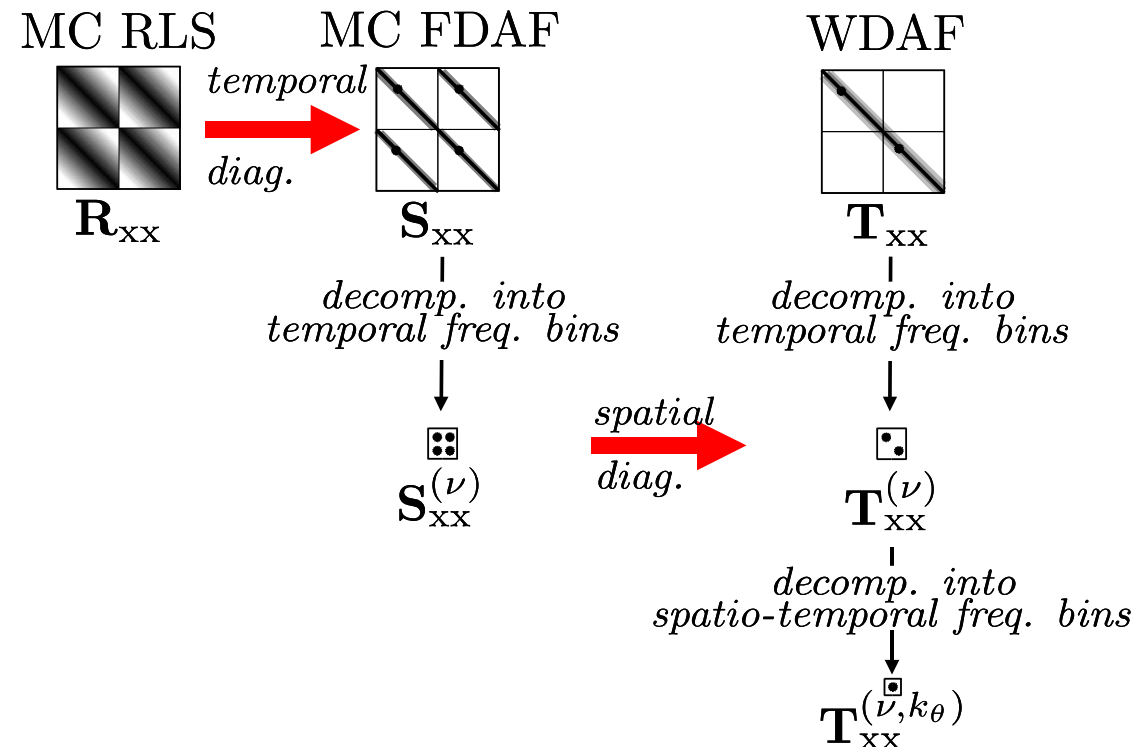




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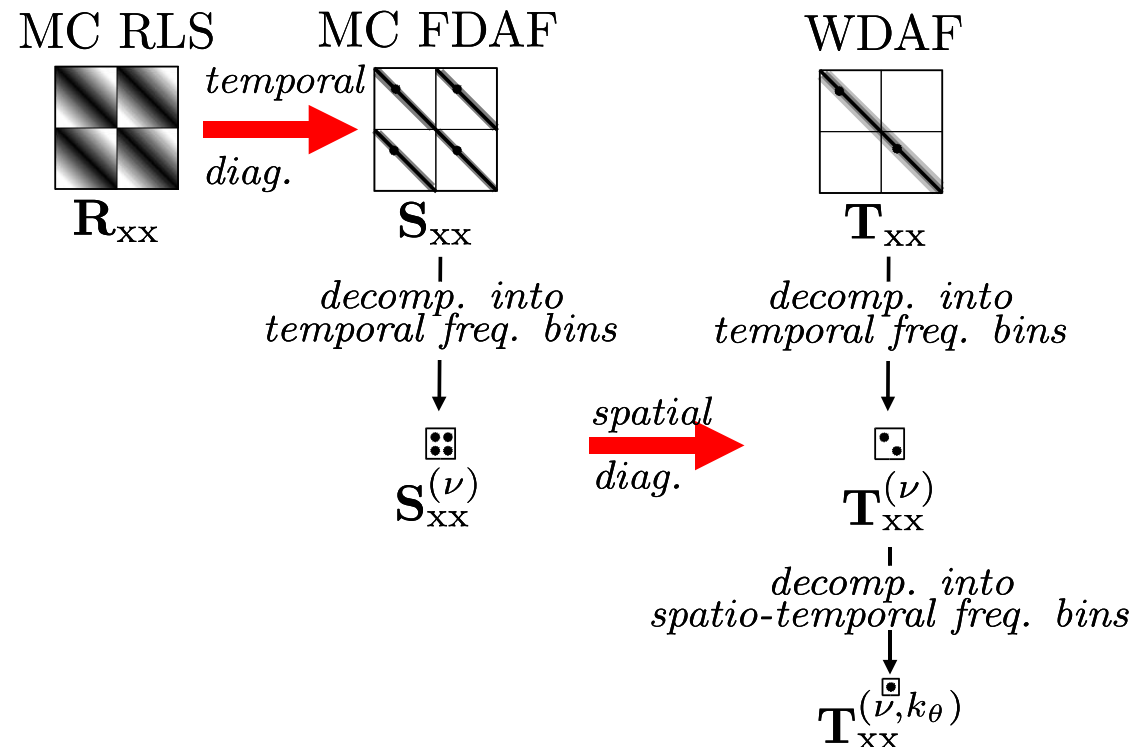
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## Desirable:

- orthogonal basis functions
- approximate decomposition among temporal frequencies as in MC FDAF
- approximate spatial decomposition
- spatio-temporal basis functions must fulfill (acoustic) wave equation

# Wave-Domain Adaptive Filtering (2)

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## Decoupling due to spatio-temporal transformation - Advantages

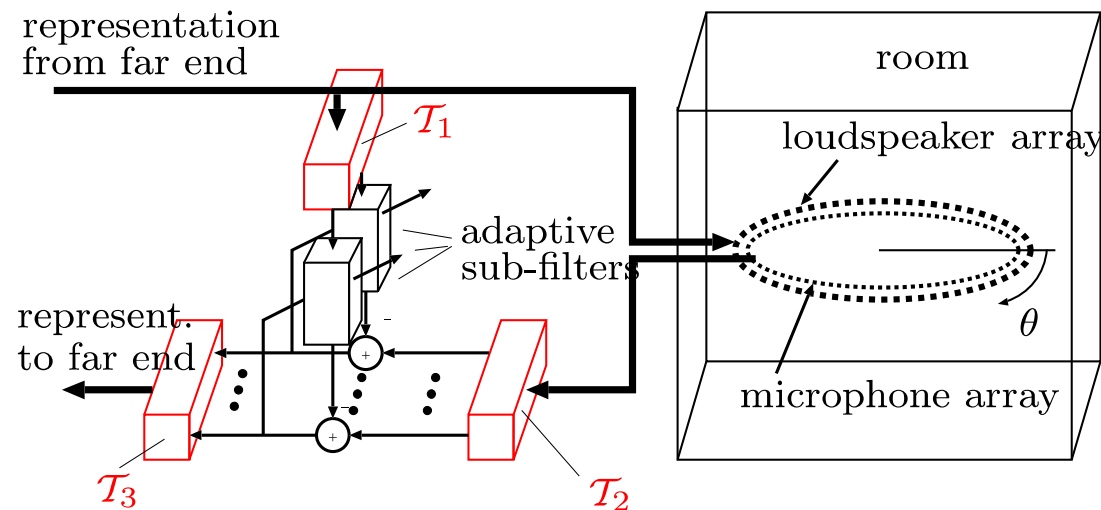
- improved convergence and very stable adaptation
- significant complexity reduction  
Example:  $P = Q = 48 \Rightarrow$  only, e.g., 70 filters instead of  $48 \cdot 48 = 2304$

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Example:  $P = Q = 48 \Rightarrow$  only, e.g., 70 filters instead of  $48 \cdot 48 = 2304$

### Example: acoustic echo cancellation



- all microphone signals simultaneously taken into account for adaptive processing
- most cross-channels in the transform domain completely negligible

# Wave-Domain Adaptive Filtering (3)

---

Transformations  $\mathcal{T}_1$ ,  $\mathcal{T}_2$ ,  $\mathcal{T}_3$  for real implementations

First approach: straightforward spatial Fourier transform ( $\rightarrow$  plane waves)

$\Rightarrow$  Problem: transducers at each point of the listening room would be needed!

# Wave-Domain Adaptive Filtering (3)

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First approach: straightforward spatial Fourier transform ( $\rightarrow$  plane waves)

$\Rightarrow$  Problem: transducers at each point of the listening room would be needed!

## Decomposition taking into account the Kirchhoff-Helmholtz Integrals

- transformations depend on array geometries
- circular arrays known to perform well in wave field analysis [Hulsebos 2001] and lead to efficient WDAF solution in cylindrical coordinates:

Example: Transformation  $\mathcal{T}_2$

$$\begin{aligned}\underline{\tilde{y}}^{(1)}(k_\theta, \omega) &= \frac{j^{1-k_\theta}}{D_R(k_\theta, \omega)} \left\{ H_{k_\theta}^{(2)'}(kR) \underline{\tilde{p}}_y(k_\theta, \omega) - H_{k_\theta}^{(2)}(kR) j\rho c \underline{\tilde{v}}_{y,n}(k_\theta, \omega) \right\}, \\ \underline{\tilde{y}}^{(2)}(k_\theta, \omega) &= \frac{-j^{1+k_\theta}}{D_R(k_\theta, \omega)} \left\{ H_{k_\theta}^{(1)'}(kR) \underline{\tilde{p}}_y(k_\theta, \omega) - H_{k_\theta}^{(1)}(kR) j\rho c \underline{\tilde{v}}_{y,n}(k_\theta, \omega) \right\}\end{aligned}$$

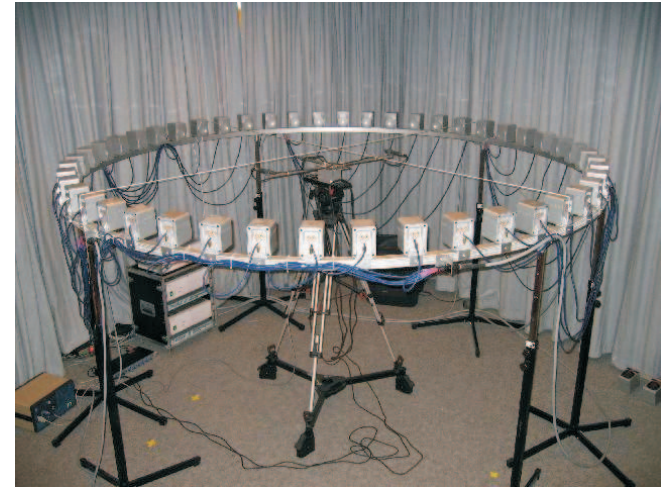
(For AEC: recording signals using pressure and pressure gradient microphone elements)

# Evaluation of WDAF for Acoustic Echo Cancellation (1)

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## Example setup:

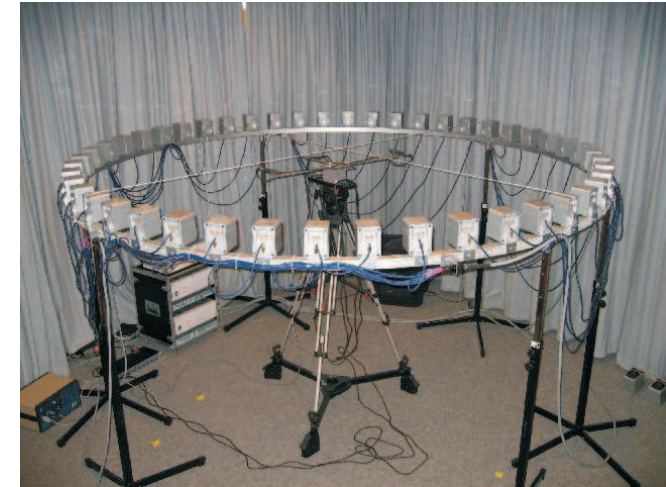
- Measured data,  $T_{60} \approx 500$  ms
- Two concentric circular arrays
- 48 loudsp.,  $R_{loudsp} = 142$  cm, spacing 19 cm
- 48 mics,  $R_{mic} = 75$  cm, spacing 9.8 cm
- Adaptation: wave-number selective FDAFs,  $L = 1024$ , overlap factor 256



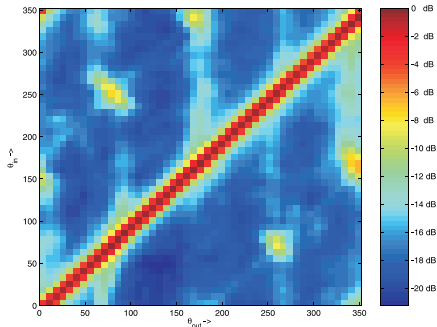
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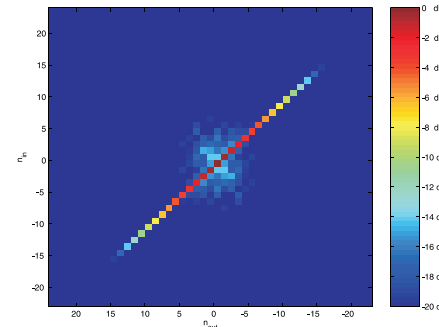
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## Loudspeaker-enclosure-microphone system in the transform domain:



spatial domain (angles)



angular wave number domain

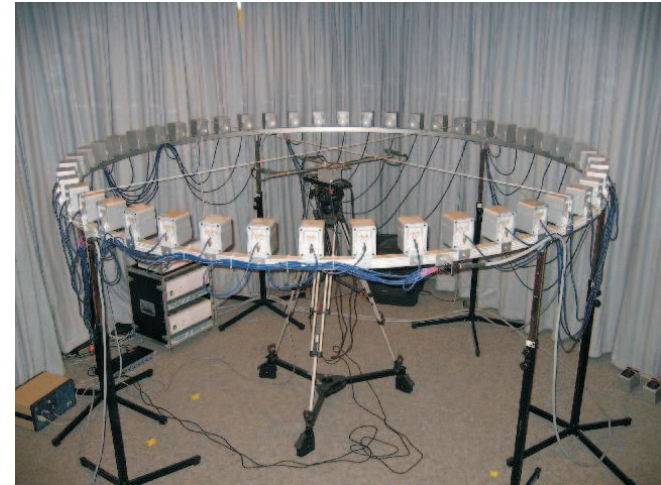
⇒ 70 (ideally 48) filters instead of  $48 \cdot 48 = 2304$  filters sufficient



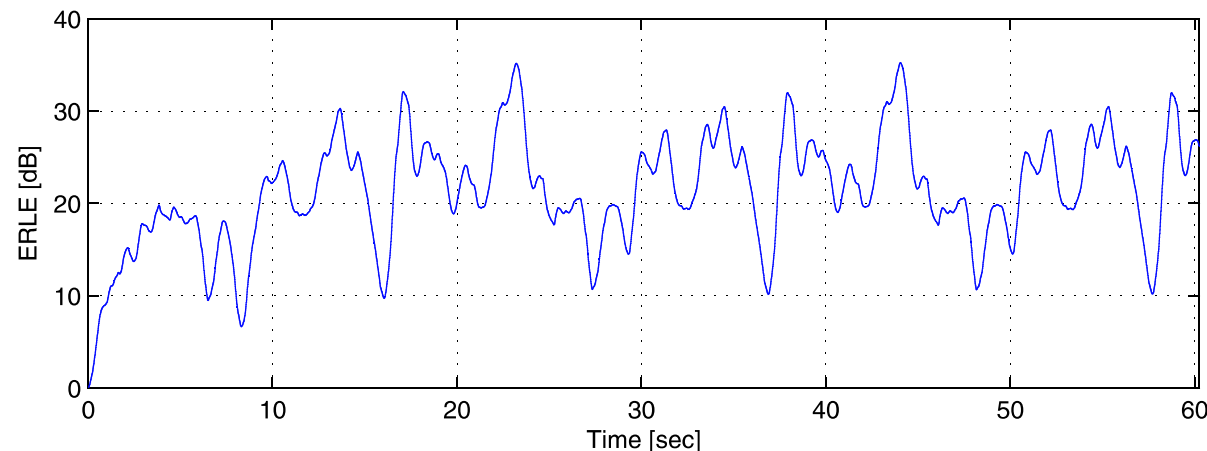
# Evaluation of WDAF for Acoustic Echo Cancellation (2)

## Example setup:

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## Echo attenuation for music:



# Summary and Outlook

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Wave-Domain Adaptive Filtering: a novel concept for efficient adaptive multichannel systems

- Spatio-temporal orthogonalization of large MIMO systems
- Very robust and fast convergence
- Low computational complexity
- Verified here for acoustic echo cancellation in a WFS-based system
- Allows integrated solutions for human-machine interfaces with wave field synthesis