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# TRINICON: A Versatile Framework for Multichannel Blind Signal Processing

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**Multimedia Communications and Signal Processing**  
Telecommunications Laboratory  
University of Erlangen-Nuremberg

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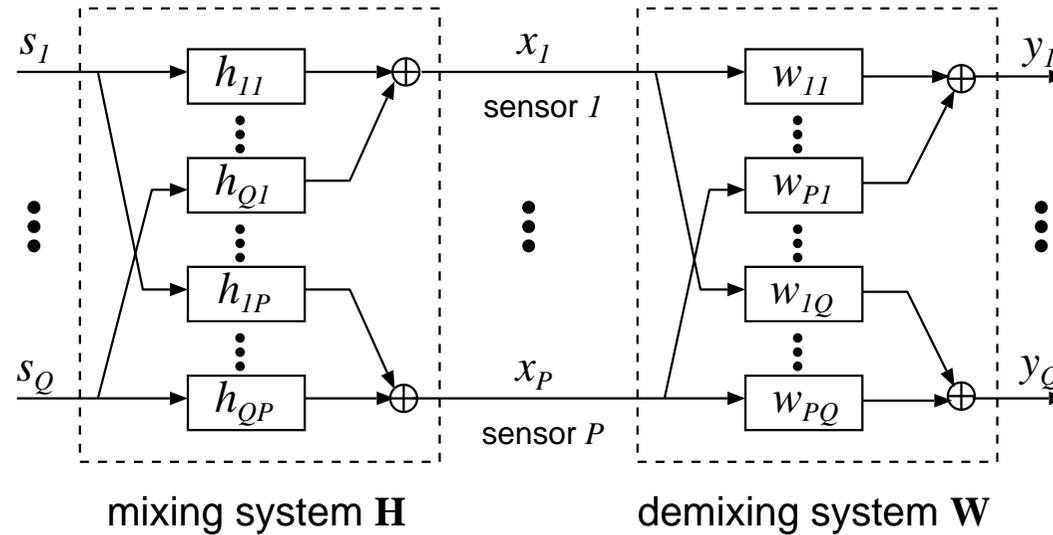
# Contents

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- Introduction: blind source separation and dereverberation
- A generic broadband algorithm
- Special cases and illustration
- Incorporation of models for spherically invariant random processes (SIRPs)
- Comparison of some examples
- Summary and outlook

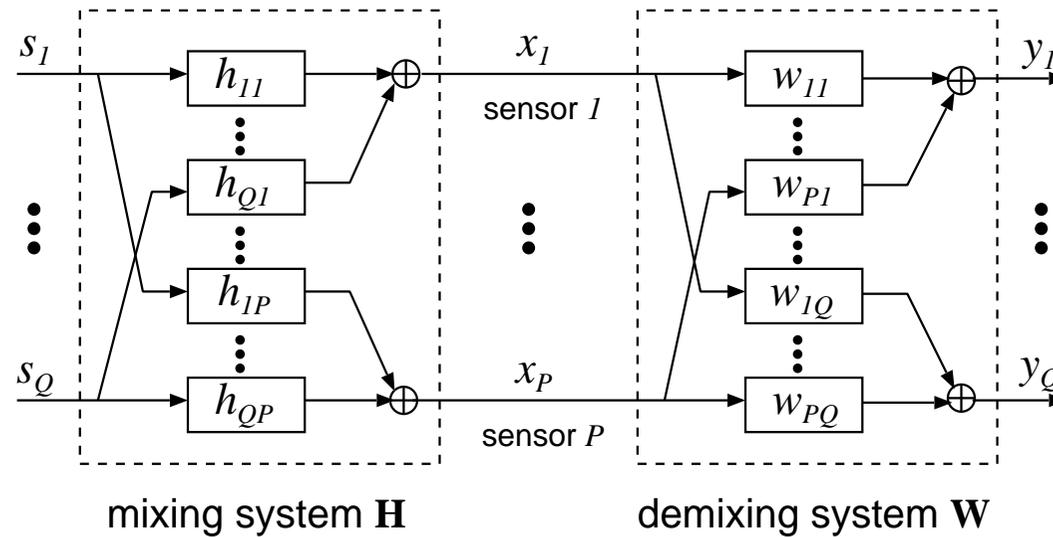
# Introduction (1)

Scenario: **MIMO FIR model** (assuming number  $Q$  of sources  $\leq$  number  $P$  of sensors)



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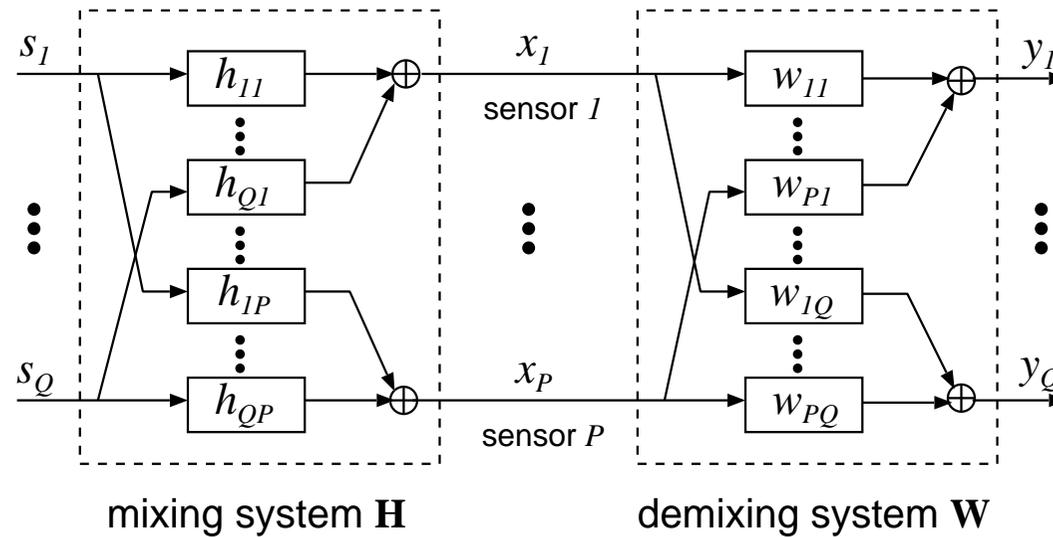
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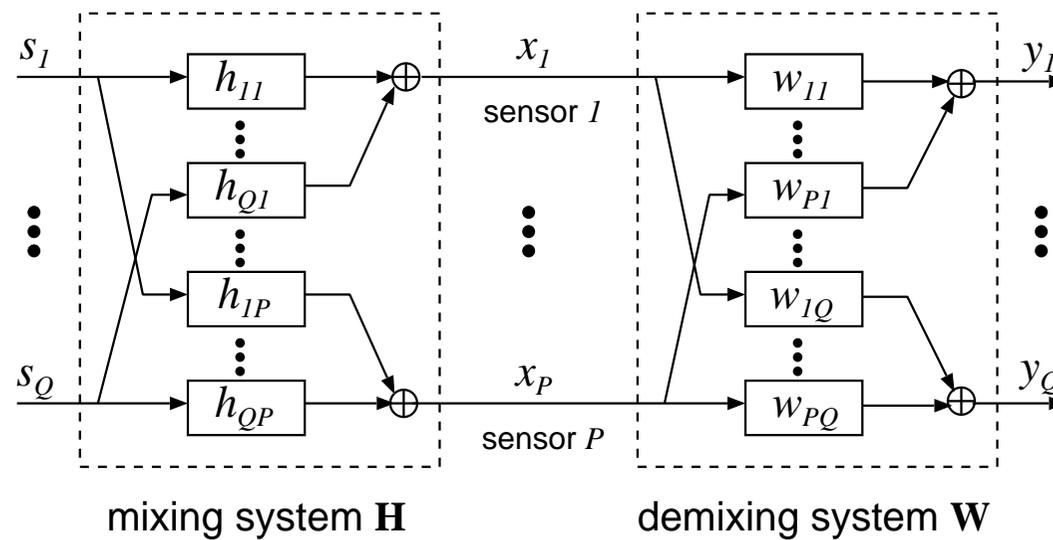


We consider here **two general classes of problems**:

- **Blind source separation (BSS) for convolutive mixtures**  
Separate signals by forcing the outputs to be mutually independent  
(output signals may be still filtered and channel-wise permuted)

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We consider here **two general classes of problems**:

- **Blind source separation (BSS) for convolutive mixtures**  
Separate signals by forcing the outputs to be mutually independent (output signals may be still filtered and channel-wise permuted)
- **Multichannel blind deconvolution  $\Rightarrow$  dereverberation**  
In addition to BSS: recover original source signals up to *scaling* and permutation

## Introduction (2)

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- Nonstationarity
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**In practice:** Combined use of properties may lead to **improved performance** and **more general applicability**.

**Here:** First rigorous derivation of a generic **broadband** adaptation algorithm

- exploiting all properties and
  - avoiding problems of narrowband approaches (permutations, circularity, ...)
- $\Rightarrow$  **TRINICON** ('**T**riple-**N** ICA for **C**onvoluteive Mixtures')

# Optimization Criterion – Motivation (1)

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**Nongaussianity:** higher-order statistics for Independent Component Analysis (ICA)

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## Current ICA approaches for BSS of instantaneous mixtures

(or for independent application on individual frequency bins, i.e., **narrowband** approaches)

- Maximum likelihood (ML)
- Minimum mutual information (MMI)
- Maximum Entropy (ME) / ‘Infomax’

It can be shown: **MMI is the most general approach** of these classes.

Mutual information [Shannon]:

$$I(Y_1, Y_2) = \int \int p(y_1, y_2) \text{ld} \left( \frac{p(y_1, y_2)}{p(y_1)p(y_2)} \right) dy_1 dy_2$$

# Optimization Criterion – Motivation (2)

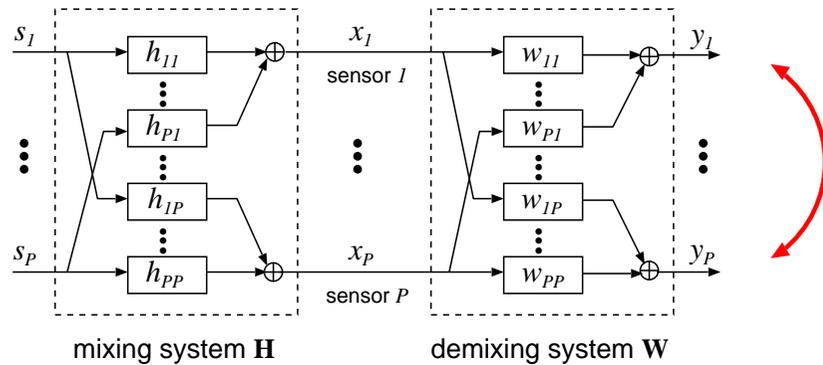
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**BSS for convolutive mixtures:**



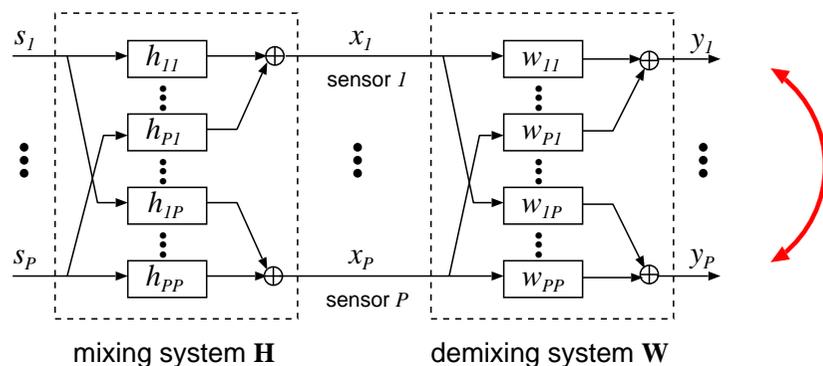
⇒ Minimize **mutual information**  
between the output channels

$$I(Y_1, Y_2) = E\{\ln(p(y_1, y_2)) - \ln(p(y_1) \cdot p(y_2))\}$$

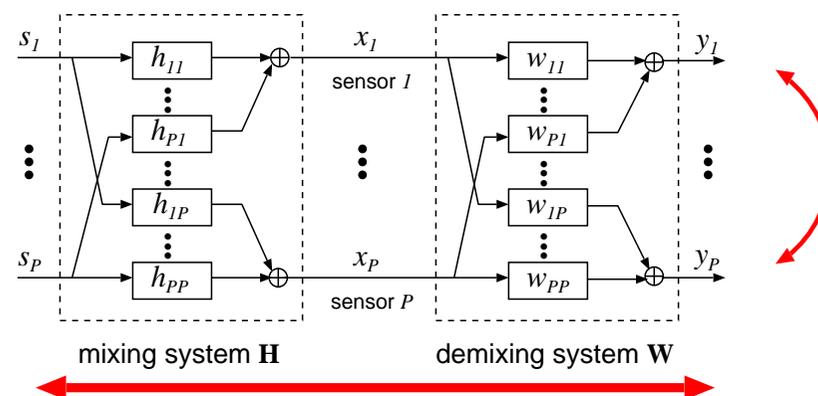
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**Multichannel Blind Deconvolution**



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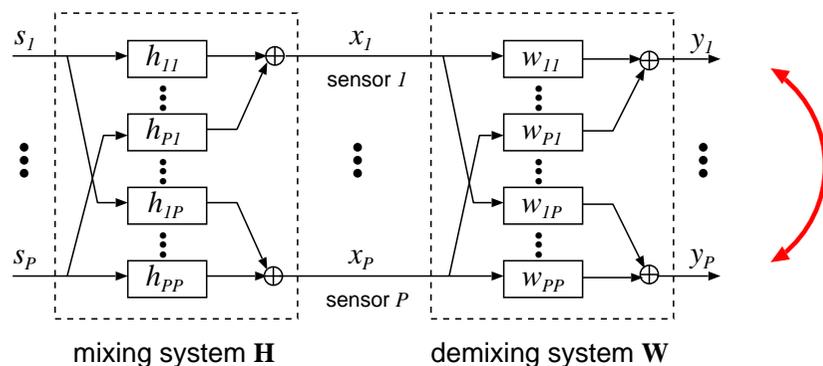
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**Most of the current approaches:**  
make outputs spatially *and* temporally independent  
**Problem for speech and audio:**  
i.i.d. assumption ⇒ whitening

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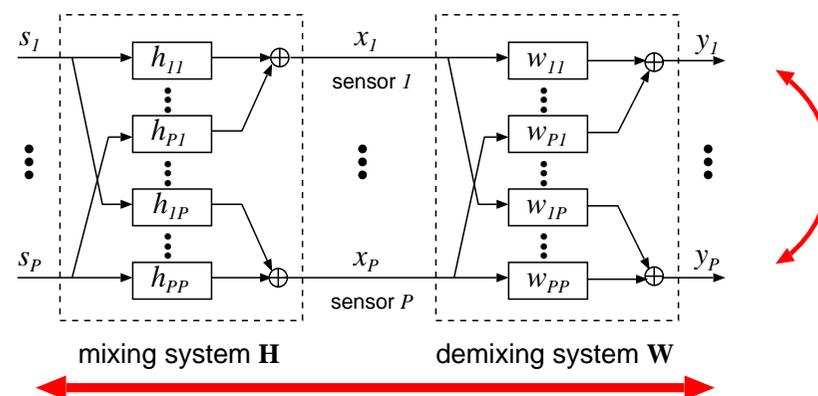
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Obvious **generalization**: factorization  $p(y_1) \cdot p(y_2) \Rightarrow$  *arbitrary 'target pdf'*

⇒ Minimize **Kullback-Leibler distance** between a certain **source model** and output

**Multichannel Blind Deconvolution**



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## General TRINICON cost function

$$\mathcal{J}(m) = - \sum_{i=0}^{\infty} \beta(i, m) \frac{1}{N} \sum_{j=0}^{N-1} \{ \log(\hat{p}_{s,PD}(\mathbf{y}(i, j))) - \log(\hat{p}_{y,PD}(\mathbf{y}(i, j))) \}$$

- $\beta$ : window function for online, offline, and block-online algorithms
- $\hat{p}_{s,PD}(\cdot)$ ,  $\hat{p}_{y,PD}(\cdot)$ : assumed or estimated *multivariate* source model PDF and output PDF, respectively.
- $\mathbf{y}(i, j)$ : concatenated length- $D$  output blocks of the  $P$  channels ( $i$ -th block, shifted by  $j$  samples),  $\mathbf{y}_q(i, j) = [y_q(iL+j), \dots, y_q(iL-D+1+j)]$

# FIR model with multiple time lags – Matrix formulation

---

**Nonwhiteness:** simultaneously optimize MIMO coefficients for  $D$  time lags

Formulation of the **linear convolution in matrix notation:**

$$\mathbf{y}_q(m, j) = [y_q(mL+j), \dots, y_q(mL-D+1+j)] = \sum_{p=1}^P \mathbf{x}_p(m, j) \mathbf{W}_{pq}(m)$$

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with the  $2L \times D$  **Sylvester matrices**

$$\mathbf{W}_{pq}(m) = \begin{bmatrix} w_{pq,0} & 0 & \dots & 0 \\ w_{pq,1} & w_{pq,0} & \ddots & \vdots \\ \vdots & w_{pq,1} & \ddots & 0 \\ w_{pq,L-1} & \vdots & \ddots & w_{pq,0} \\ 0 & w_{pq,L-1} & \ddots & w_{pq,1} \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \dots & 0 & w_{pq,L-1} \\ 0 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & \dots & 0 & 0 \end{bmatrix} \cdot$$

# General Coefficient Update

Natural gradient  $\mathbf{W}\mathbf{W}^H \nabla_{\mathbf{W}} \mathcal{J}$  of the cost function as **generic coefficient update**:

$$\Delta \mathbf{W}(m) = \frac{2}{N} \sum_{i=0}^{\infty} \beta(i, m) \sum_{j=0}^{N-1} \mathbf{W}(i) \mathbf{y}^H(i, j) \{ \Phi_{s,PD}(\mathbf{y}(i, j)) - \Phi_{y,PD}(\mathbf{y}(i, j)) \}$$

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**To select a practical algorithm:**

- 'desired' score function (hypothesized)

$$\Phi_{s,PD}(\mathbf{y}(i, j)) = -\frac{\partial \log \hat{p}_{s,PD}(\mathbf{y}(i, j))}{\partial \mathbf{y}(i, j)}$$

where the model (i.e., desired) PDF is **factorized among the channels** ( $\Rightarrow$  BSS) and/or **factorized among a certain number of time lags** ( $\Rightarrow$  full or partial MCBD)

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**How to obtain these sequences of high-dimensional multivariate PDFs?**

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**SOS case** exploiting only non-stationarity and non-whiteness  
by assuming **multivariate Gaussian** PDFs in both score functions:

$$\hat{p}_D(\mathbf{y}_p(i, j)) = \frac{1}{\sqrt{(2\pi)^D \det(\mathbf{R}_{\mathbf{y}_p \mathbf{y}_p}(i))}} e^{-\frac{1}{2} \mathbf{y}_p(i, j) \mathbf{R}_{\mathbf{y}_p \mathbf{y}_p}^{-1}(i) \mathbf{y}_p^H(i, j)}$$

$$\Delta \mathbf{W}(m) = 2 \sum_{i=0}^{\infty} \beta(i, m) \mathbf{W} \left\{ \hat{\mathbf{R}}_{\mathbf{y}\mathbf{y}} - \hat{\mathbf{R}}_{\mathbf{s}\mathbf{s}} \right\} \hat{\mathbf{R}}_{\mathbf{s}\mathbf{s}}^{-1}$$

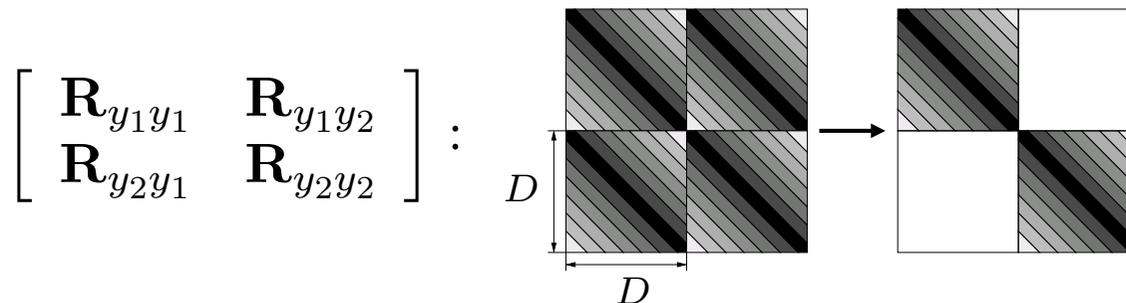
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- Generic SOS-based BSS:  $\hat{\mathbf{R}}_{\mathbf{s}\mathbf{s}} = \text{bdiag}_D \hat{\mathbf{R}}_{\mathbf{y}\mathbf{y}}$



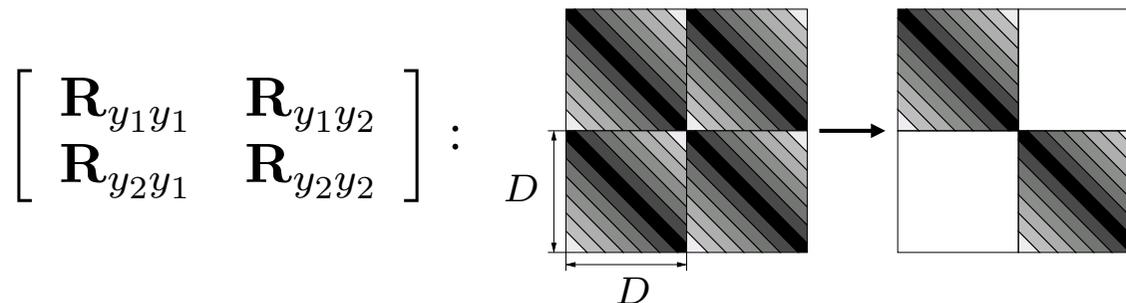
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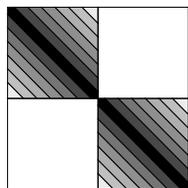
- Inherent RLS-like normalization  $\Rightarrow$  Robust adaptation

## Special Cases and Illustration – SOS case (2)

$$\Delta \mathbf{W}(m) = 2 \sum_{i=0}^{\infty} \beta(i, m) \mathbf{W} \left\{ \hat{\mathbf{R}}_{yy} - \hat{\mathbf{R}}_{ss} \right\} \hat{\mathbf{R}}_{ss}^{-1}$$

Desired correlation matrices  $\hat{\mathbf{R}}_{ss}$  for BSS and dereverberation:

(a) **BSS**



$$\hat{\mathbf{R}}_{ss} = \text{bdiag}_D \hat{\mathbf{R}}_{yy}$$

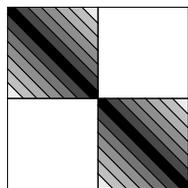
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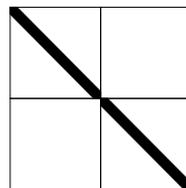
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(b) **MCBD**



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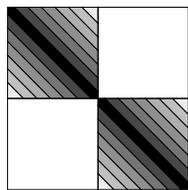
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⇒ **undesirable for speech  
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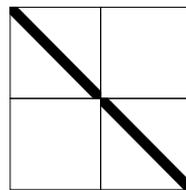
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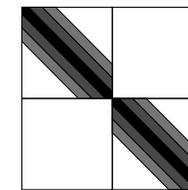
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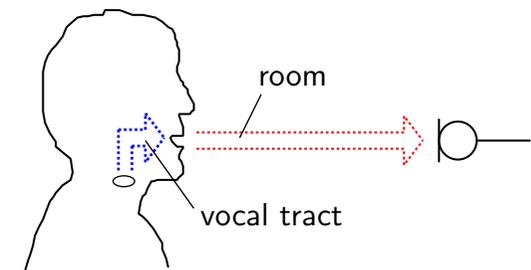
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(c) **MCBPD**



remove only the influence  
 of the room  
 $\Rightarrow$  **vocal tract untouched**



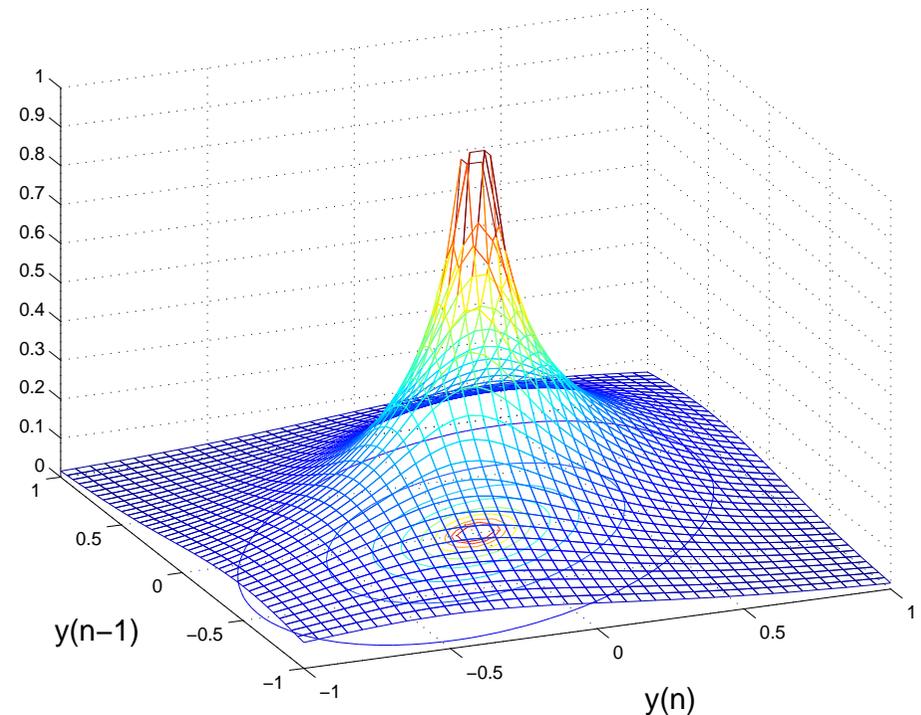
# Models for Spherically Invariant Processes (SIRPs) in TRINICON

SIRPs are described by multivariate PDFs of the form (with suitable function  $f_D$ ):

$$\hat{p}_D(\mathbf{y}_p) = \frac{1}{\sqrt{\pi^D \det(\hat{\mathbf{R}}_{pp})}} f_D \left( \mathbf{y}_p \hat{\mathbf{R}}_{pp}^{-1} \mathbf{y}_p^H \right)$$

**Several attractive properties:**

- Good model for speech signals
- Closed-form representation



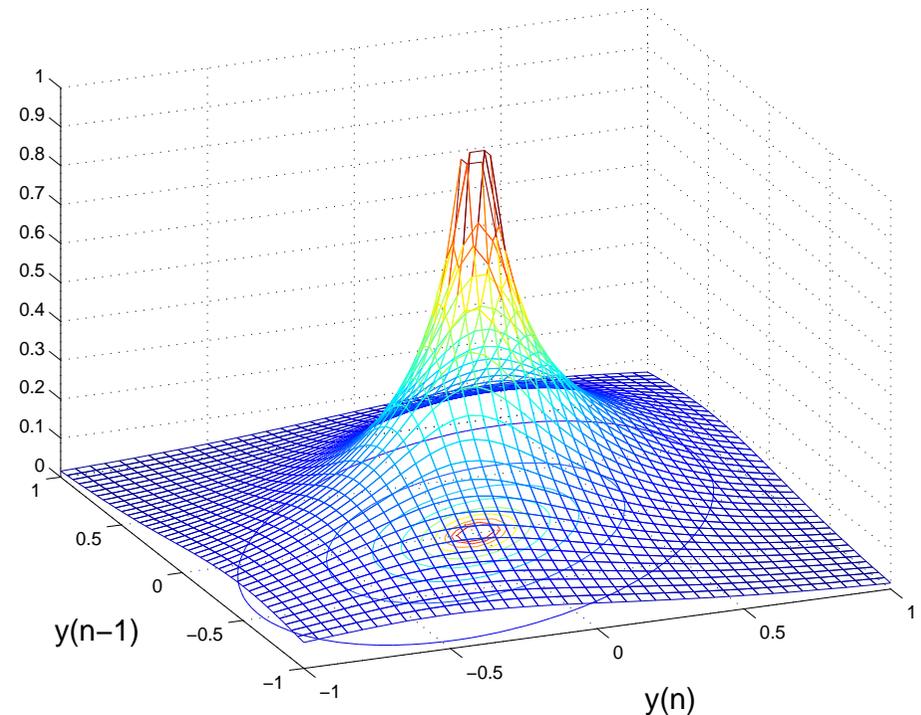
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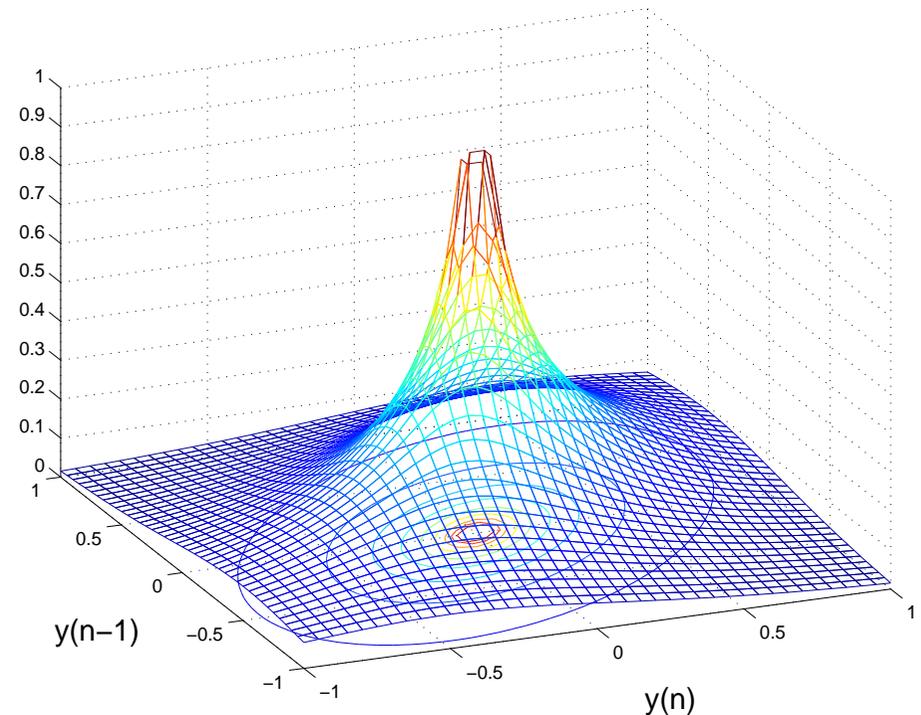
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- Multivariate PDFs can be derived analytically from corresponding univariate PDFs



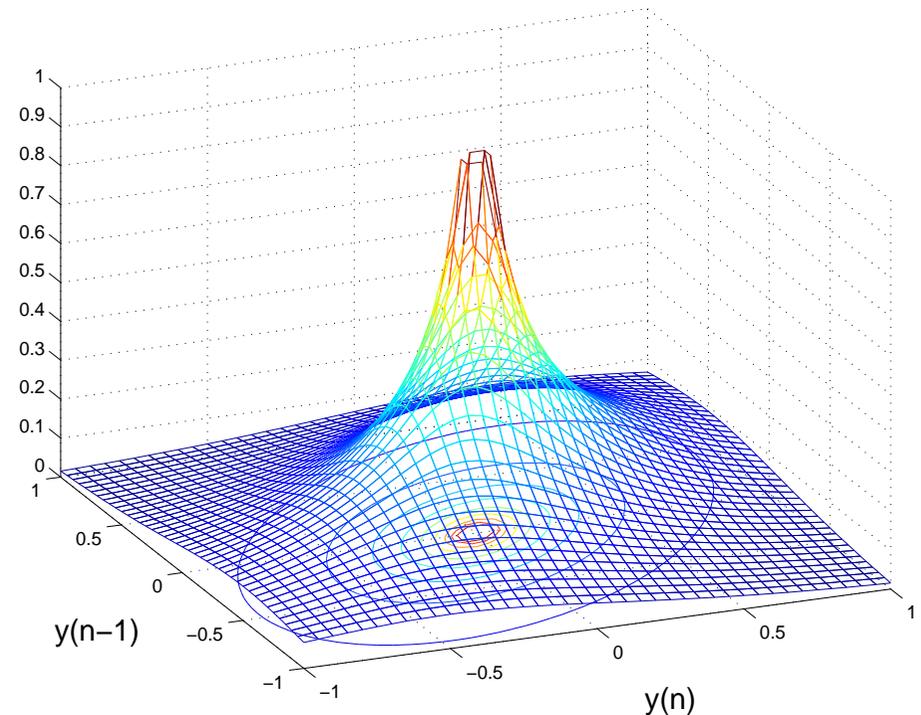
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## Several attractive properties:

- Good model for speech signals
- Closed-form representation
- Reduced number of parameters to estimate for BSS or Dereverberation
- Multivariate PDFs can be derived analytically from corresponding univariate PDFs
- Incorporation into TRINICON leads to inherent stepsize normalization of the update equation



# Incorporation of SIRPs into Generic BSS

**BSS:** coefficient update for 2 sources with SIRPs reads

$$\Delta \mathbf{W}(m) = \sum_{i=0}^m \beta(i, m) \mathbf{W}(i) \begin{bmatrix} \mathbf{0} & \tilde{\mathbf{R}}_{y_1 y_2} \mathbf{R}_{y_2 y_2}^{-1} \\ \tilde{\mathbf{R}}_{y_2 y_1} \mathbf{R}_{y_1 y_1}^{-1} & \mathbf{0} \end{bmatrix}$$

# Incorporation of SIRPs into Generic BSS

**BSS:** coefficient update for 2 sources with SIRPs reads

$$\Delta \mathbf{W}(m) = \sum_{i=0}^m \beta(i, m) \mathbf{W}(i) \begin{bmatrix} \mathbf{0} & \tilde{\mathbf{R}}_{y_1 y_2} \mathbf{R}_{y_2 y_2}^{-1} \\ \tilde{\mathbf{R}}_{y_2 y_1} \mathbf{R}_{y_1 y_1}^{-1} & \mathbf{0} \end{bmatrix}$$

- **RLS-like normalization** (by lagged auto-correlation matrices  $\mathbf{R}_{y_q y_q}$ )
- Matrices  $\tilde{\mathbf{R}}_{y_p y_q}$  of cross-relations include nonlinear terms derived from multivariate PDFs:

$$\tilde{\mathbf{R}}_{y_p y_q}(i) = \frac{1}{N} \sum_{j=0}^{N-1} \phi_D \left( \mathbf{y}_q(i, j) \mathbf{R}_{y_q y_q}^{-1}(i) \mathbf{y}_q^H(i, j) \right) \mathbf{y}_p^H(i, j) \mathbf{y}_q(i, j),$$
$$\phi_D(s) = -\frac{f'_D(s)}{f_D(s)}$$

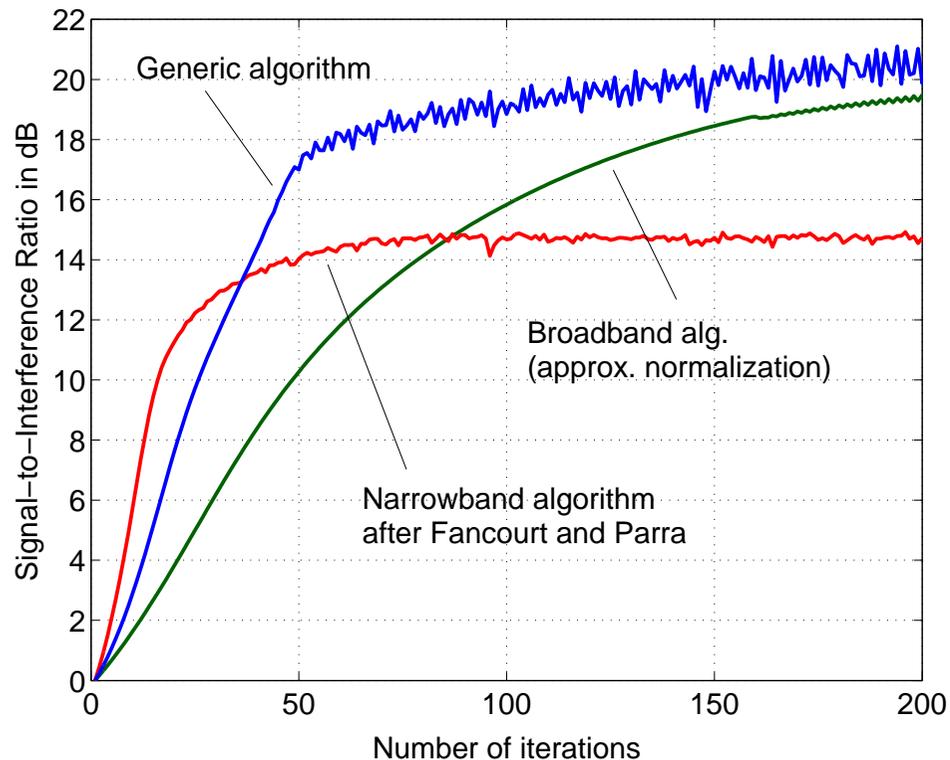
- **HOS-SIRP realizations:**  $\phi_D(s)$  may be derived analytically from the univariate PDF

# Examples

- **BSS performance:**

Conditions: Reverberation time  $T_{60} \approx 200ms$ ,  $2 \times 2$  case, speech signals, microphone spacing  $16cm$ , sampling rate  $16kHz$ , estimation of  $\mathbf{R}_{yy}$  by correlation method

## SOS Algorithms ( $L = 1024$ )

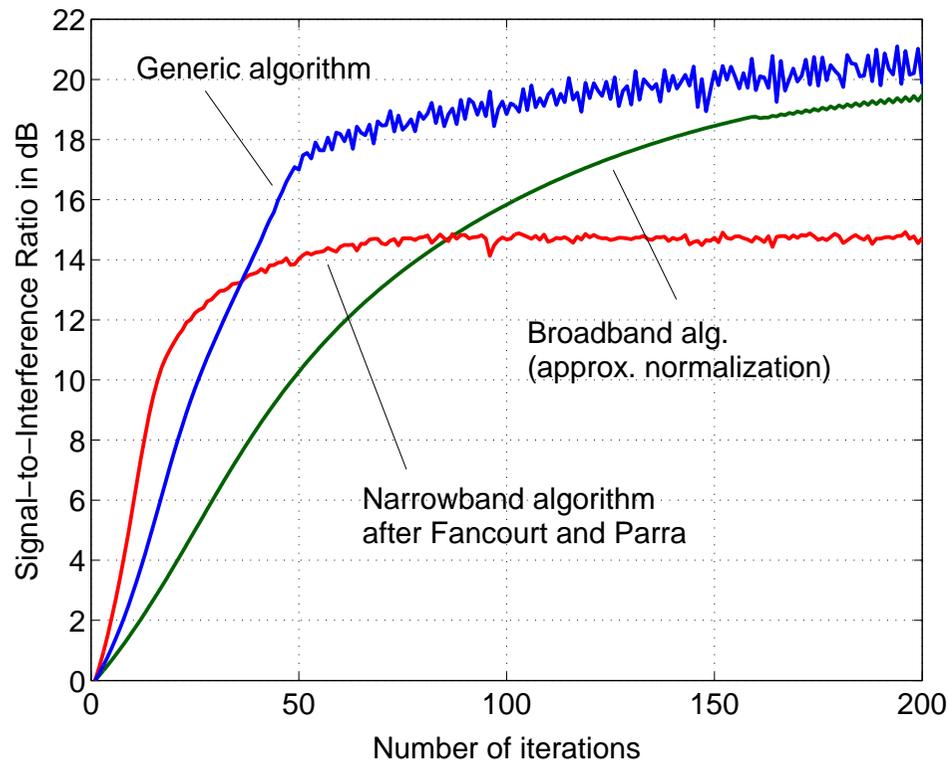


# Examples

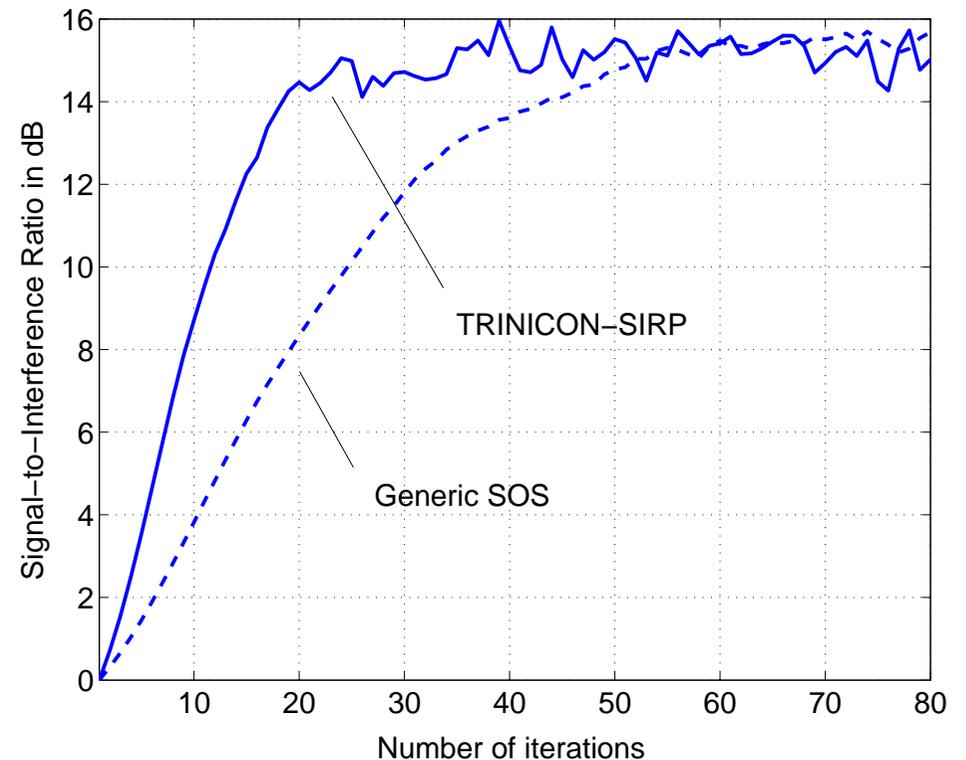
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## SOS Algorithms ( $L = 1024$ )



## Generic SOS vs. TRINICON

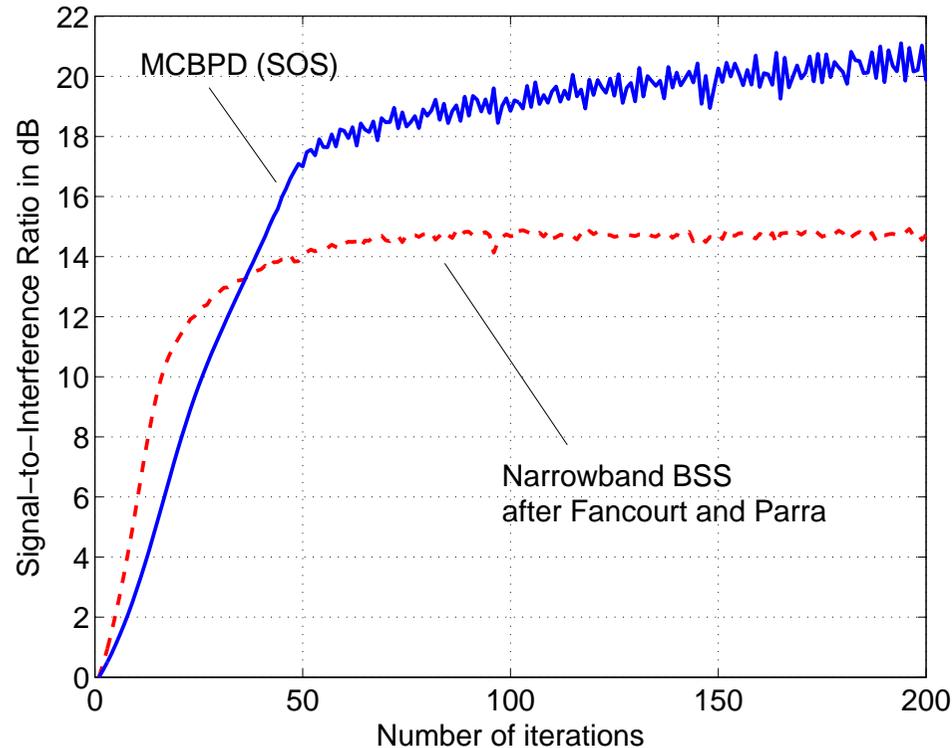


## Examples (2)

- **SOS-dereverberation performance:**

Conditions: Reverberation time  $T_{60} \approx 200ms$ ,  $2 \times 2$  case, speech signals, microphone spacing  $16cm$ , unmixing filter length 1024 taps, sampling rate 16kHz, estimation of  $\mathbf{R}_{yy}$  by correlation method

### SIR improvement

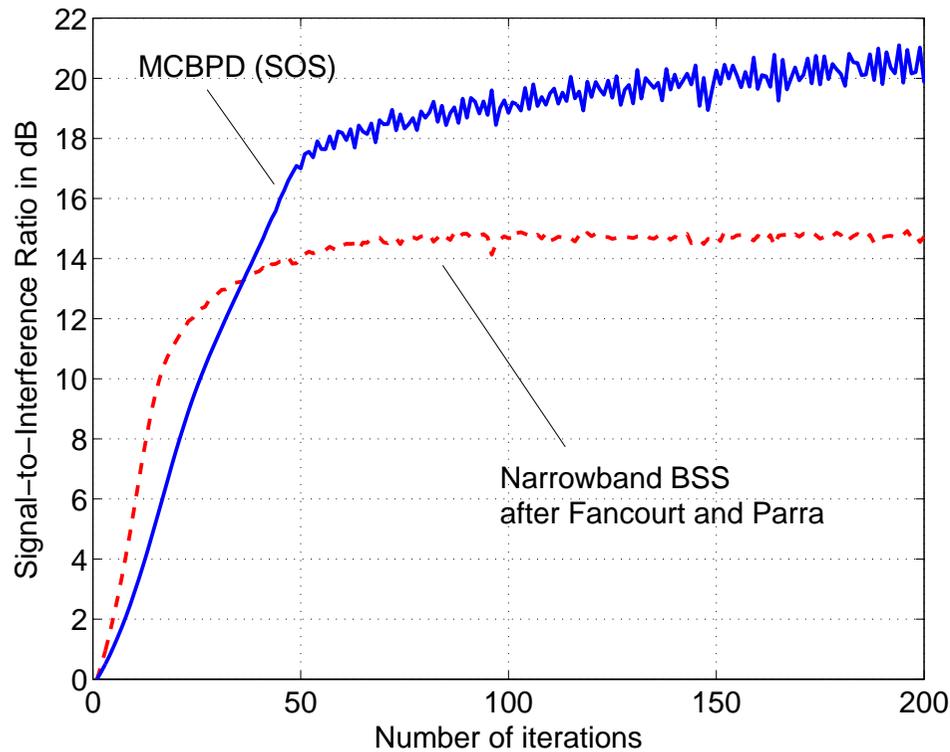


## Examples (2)

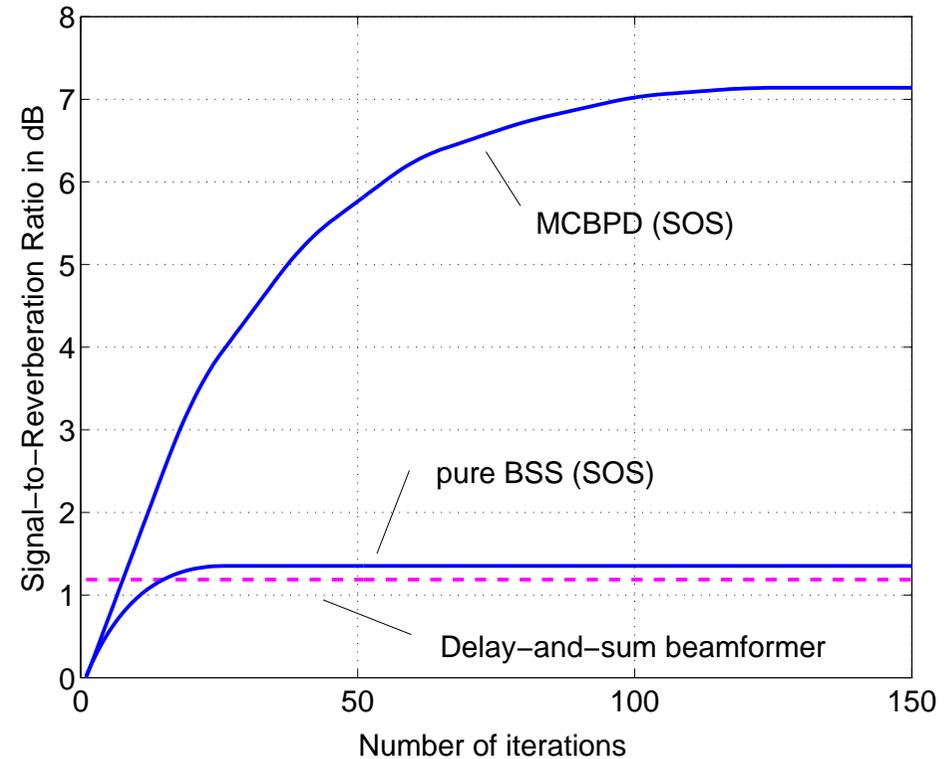
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### SIR improvement



### SRR improvement



# Summary and Outlook

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- Versatile framework for blind MIMO signal processing exploiting **nongaussianity, nonwhiteness, and nonstationarity** in a rigorous way
- Various novel algorithms can be derived from it (time-domain and frequency-domain)
- Examples show: **separation gain more than  $20dB$ , dereverberation gain more than  $7dB$**
- This broadband approach has led to efficient realtime BSS on a laptop PC
- More sophisticated source models (e.g., HMM-based) may be incorporated in the framework